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Brief Discussion:

Fig.UW-13.2 Non-Permissible heads, ASME VIII-1, by Finite Element Analysis

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Key Design Engineering is a Canadian engineering firm located in Waterloo, Ontario, that specializes in ASME Code calculations and Canadian Registration Number (CRN) submissions:

- **ASME Code Calculations** per ASME VIII-1 & ASME B31.3 for Pressure Vessels, Fittings, & Piping systems as applicable.
- **Canadian Registration Number (CRN)**: preparation of documentation for submission of pressure vessels, fittings, or pressure piping for registration in one Jurisdiction or Canada-wide.
- **Finite Element Analysis (FEA)** of Pressure Vessels and Fittings in accordance with ASME VIII-2, in compliance with Jurisdictional requirements.

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**Sample Project.
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Summary:

Finite Element Analysis (FEA) is used to investigate reasons why ASME VIII-1, FIG.UW-13.2, does not permit certain joint configurations for the attachment of welded unstayed flat heads:

1. **Joint Orientation**: The eccentrically attached weld allows the joint to open under pressure.
2. **Fatigue Life**: The peak stress created at the weld root limits the fatigue life.
3. **Weld size**: The weld size is insufficient to satisfy the Code's geometric requirements.

Introduction:

ASME VIII-1 lists various examples of permissible flat welded-head configurations in Fig.UG-34 & Fig.UW-13.2. Why are the following three joints listed as “Non-Permissible” in Fig.UW-13.2?

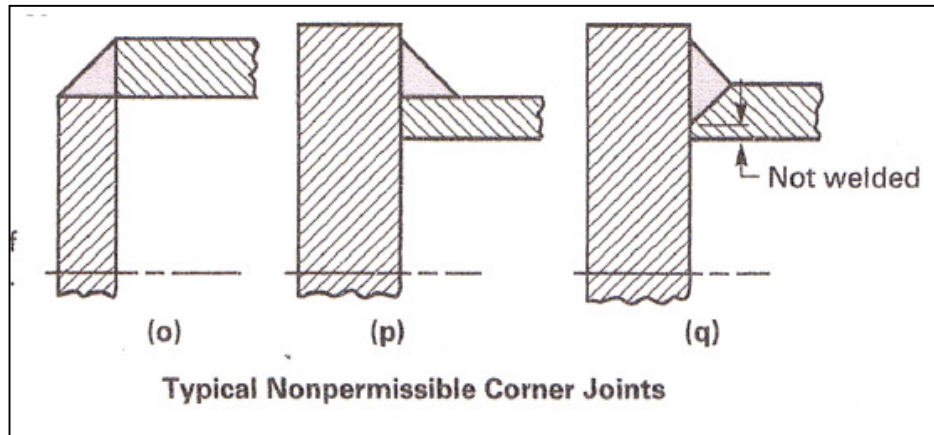


Figure UW-13.2

Approach:

The three non-permissible configurations presented in Fig.UW-13.2 are analyzed: o, p, & q. For comparison, an analysis is also performed on Fig.UG-34(e), which is permissible.

General Setup:

Code of Construction:	ASME VIII-1, 2007ed, 2009b
Design Conditions:	1,000 psi @ 650F
Material:	Shell: SA-312 TP304 Flat head: SA-240 304
Corrosion Allowance:	N/A
Mesh Error:	Max 5%, per ABSA guideline
FEA Interpretation:	ASME VIII-2, 2007, Part 5
E (weld quality)	1.0, per table UW-12, corner joint
Thicknesses	Head and shell thicknesses sized per Classical Calculations, attached to this discussion.

Results: Nonpermissible Configurations

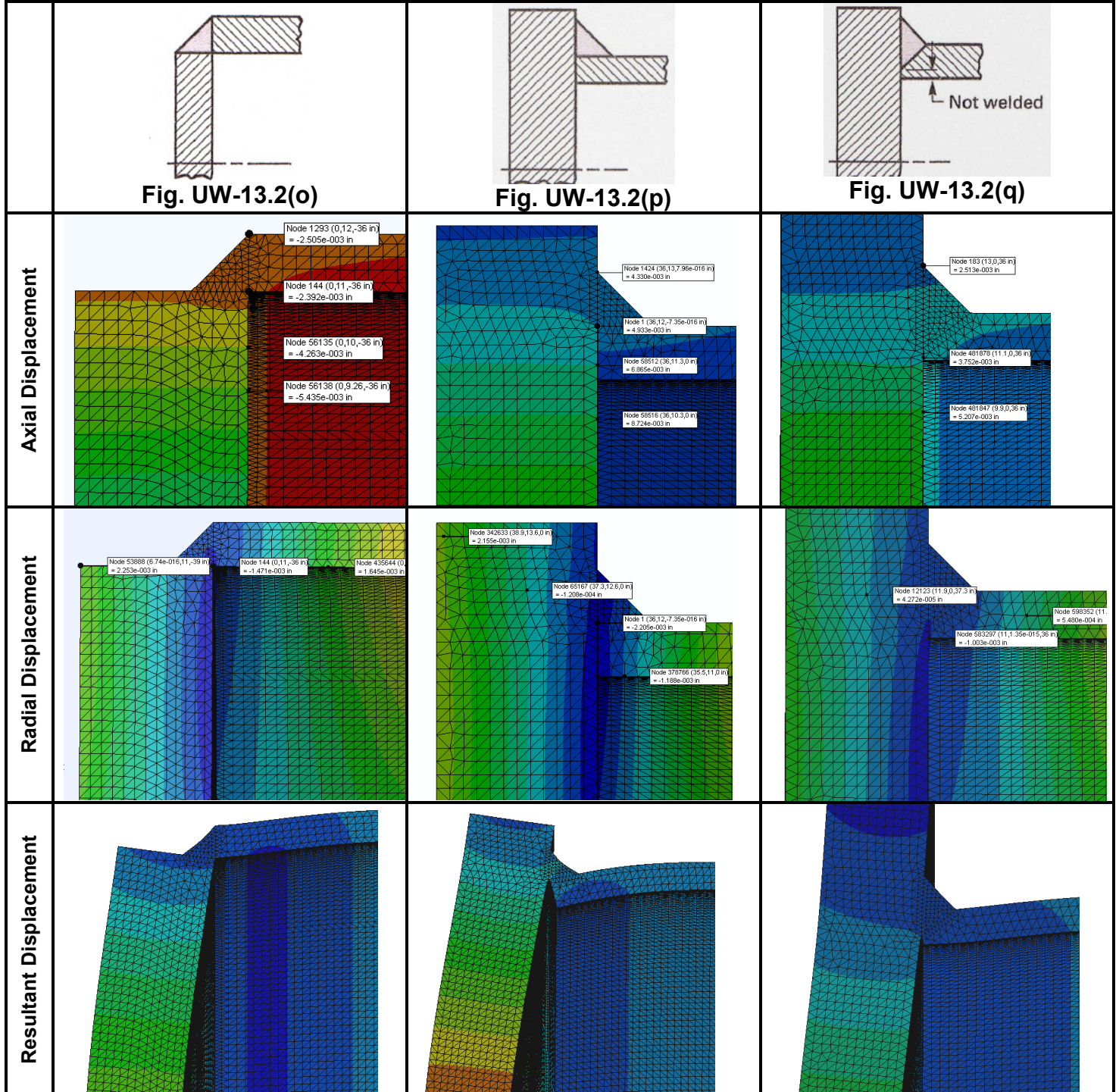
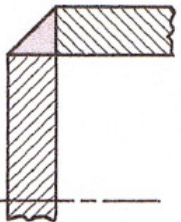
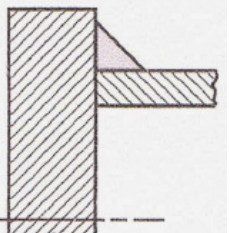
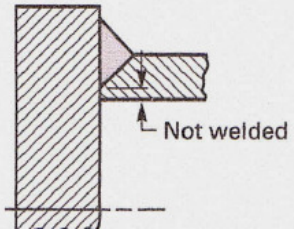
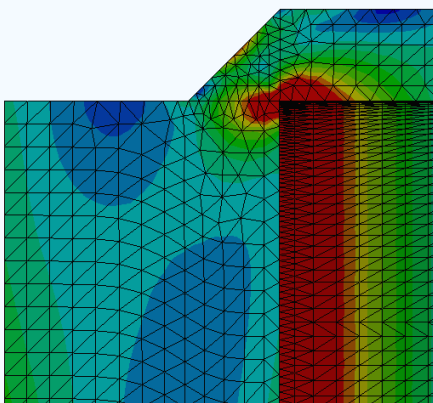
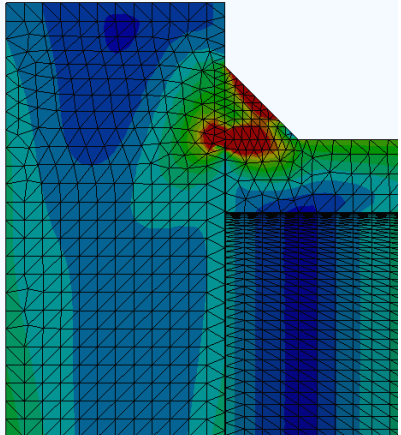
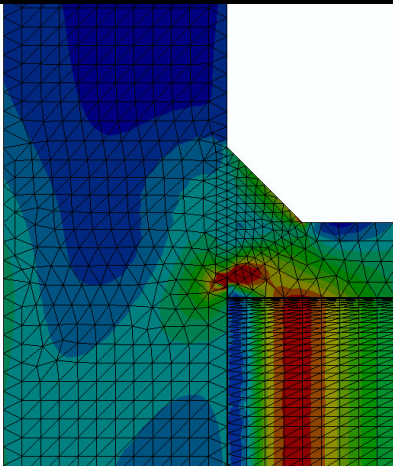


Table continued from previous page

	 <p>Fig. UW-13.2(o)</p>	 <p>Fig. UW-13.2(p)</p>	 <p>Fig. UW-13.2(q)</p>
Resultant Von Mises Stress plots	 <p>Peak stress = $3.2xS$, at the inside corner. Expected life = $1.05E+06$ cycles</p>	 <p>Peak stress = $3.6xS$, at the weld root, forming a line around the circumference. Expected life = $7.87E+05$ cycles</p>	 <p>Peak stress = $2.1xS$, at the root, around the circumference of the part. Expected life = $5.74E+06$ cycles</p>

Referring to the preceding results, note the following:

- For the *Resultant Displacement* plots, the colour display has been capped at $2.076e-002$ in. for comparison between the three configurations.
- The *Resultant Displacement* plots above are shown deformed at a scale of 100x, but both the *Axial* and *Radial displacement* plots are shown undeformed.
- For the *Von Mises Stress Plots*, the colour display has been capped at the allowable stress for stainless SA-240 304 @ 650F, which also corresponds to P_m , the membrane allowable stress.

Results: Permissible Configuration

An analysis is run for the unstayed flat-head of FIG.UG-34(e), using the same design conditions.

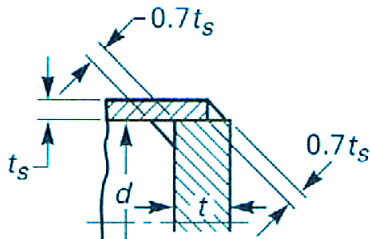
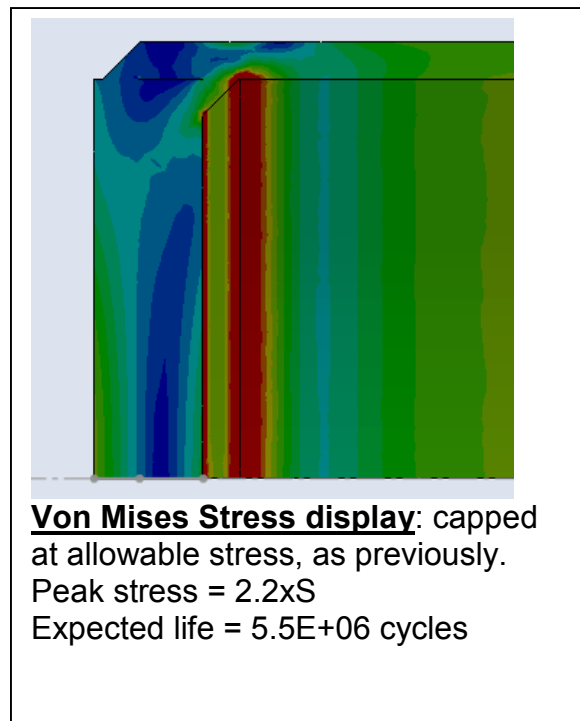
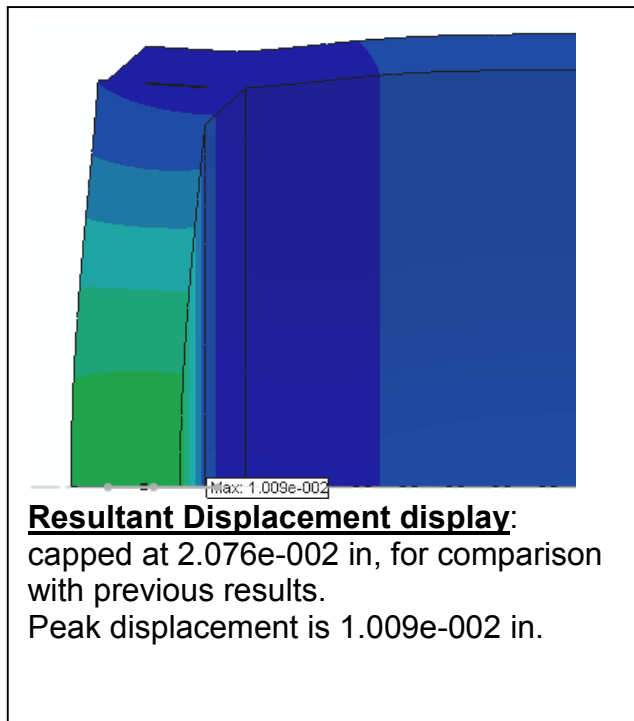


Fig. UG-34(e)





Observations:

It is immediately clear that for the two Nonpermissible cases (o) & (p), there isn't sufficient weld to satisfy the geometric requirement of the Code (VIII-1 UW-13(e)(5)). Also, the *Radial Displacement* Plot for case (o) shows a hinge developing at the weld's root, which makes it vulnerable to fatigue failure. However, the *Resultant Displacement* plots for cases (p) & (q) highlight the main underlying problem with these configurations. It is the weld's eccentricity relative to the main pressure-retaining component, the shell. In a permissible joint, a flat head will normally cause a moment to form in its attached shell, as can be observed in case (e) from Fig. UG-34 above. What sets these two cases apart is that the deformation causes an opening up of the joint. Rather than it being a self-limiting effect, such as relieves local peak stresses, it has a ratcheting effect that leads to premature failure under cyclic loading. In contrast, the permissible joint investigated has very low deflection both at the centre of the head and through the weld. While it also displays a peak stress at the weld root, the joint remains closed and any plasticity will be local to relieve the geometric stress concentrations at that point. The fatigue-life of the joint is greatly affected by the weld finish quality, but even this theoretical treatment shows that configuration (p) most severely limits the expected life cycles. An additional practical consideration is crevice corrosion, which could seriously impact stainless steel in configurations (p) & (q).

Additional References:

- A. ASME VIII-1, UW-13 (e)(5) speaks to the reasons for these joints being nonpermissible:
- **Weld Size:** The total weld dimension through the joint (throat) is less than the thickness of the pressure part to which it is attached, whether it be the shell, head or other component.
 - **Eccentricity:** The weld creates a joint that is attached eccentric to the pressure part.
- B. Compress Calculations per ASME VIII-1, 2007 ed, 2009b for UG-34(e) unstayed flat-head. It was used for determining head and shell thickness.

Welded Cover Fig.UG-34(e)**ASME Section VIII Division 1, 2007 Edition, A09 Addenda**

Component: Welded Cover
 Material specification: SA-240 304 (II-D p. 90, ln. 4)
 Rated MDMT per UHA-51(d)(1)(a) = -320 °F

Internal design pressure: $P = 1000$ psi @ 650 °F

External design pressure: $P_e = 15$ psi @ 650 °F

Corrosion allowance: Inner C = 0" Outer C = 0"

Design MDMT = -20 °F No impact test performed
 Rated MDMT = -320 °F Material is not normalized
 Material is not produced to Fine Grain Practice
 PWHT is not performed

Radiography: Category A joints - Seamless No RT

Estimated weight: New = 394.9 lb corr = 394.9 lb

Head diameter, $d = 24$ "

Cover thickness, $t = 3.01$ "

Factor C from Fig. UG-34, sketch (b-2), (e through g)

$$\begin{aligned} C &= 0.33 \cdot t_r / t_s \\ &= 0.33 \cdot 0.7692 / 1 \\ &= 0.2538 \end{aligned}$$

Design thickness, (at 650 °F) UG-34 (c)(2)

$$\begin{aligned} t &= d \cdot \text{Sqr}(C \cdot P / (S \cdot E)) + \text{Corrosion} \\ &= 24 \cdot \text{Sqr}(0.2538 \cdot 1,000 / (16,200 \cdot 1)) + 0 \\ &= 3.004" \end{aligned}$$

Maximum allowable working pressure, (at 650 °F)

$$\begin{aligned} C &= 0.33 \cdot t_r / t_s \\ &= 0.33 \cdot 0.7708 / 1 \\ &= 0.2544 \end{aligned}$$

$$\begin{aligned} \text{MAWP} &= (S \cdot E / C) \cdot (t / d)^2 - P_s \\ &= (16,200 \cdot 1 / 0.2543645) \cdot (3.01 / 24)^2 - 0 \\ &= 1,001.91 \text{ psi} \end{aligned}$$

Maximum allowable pressure, (At 70 °F)

$$\begin{aligned} C &= 0.33 \cdot t_r / t_s \\ &= 0.33 \cdot 0.7708 / 1 \\ &= 0.2544 \end{aligned}$$

$$\begin{aligned} \text{MAP} &= (S \cdot E / C) \cdot (t / d)^2 \\ &= (20,000 \cdot 1 / 0.2543645) \cdot (3.01 / 24)^2 \\ &= 1,236.93 \text{ psi} \end{aligned}$$

Design thickness for external pressure, (at 650 °F) UG-34(c)(2)

$$\begin{aligned} t &= d \cdot \text{Sqr}(C \cdot P_e / (S \cdot E)) + \text{Corrosion} \\ &= 24 \cdot \text{Sqr}(0.33 \cdot 15 / (16,200 \cdot 1)) + 0 \\ &= 0.4195" \end{aligned}$$

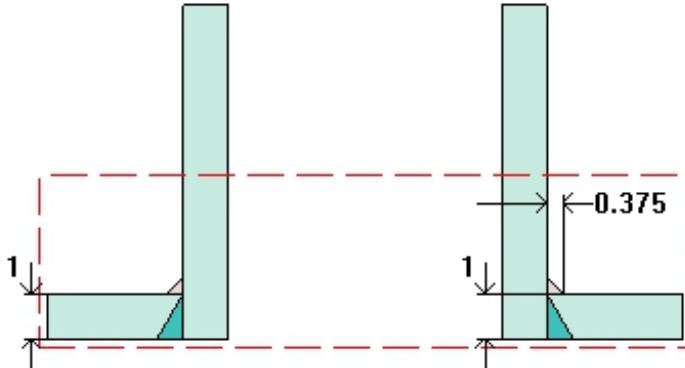
Maximum allowable external pressure, (At 650 °F)

$$\begin{aligned} \text{MAEP} &= (S \cdot E / C) \cdot (t / d)^2 \\ &= (16,200 \cdot 1 / 0.33) \cdot (3.01 / 24)^2 \\ &= 772.17 \text{ psi} \end{aligned}$$

Nozzle #1 (N1)**ASME Section VIII Division 1, 2007 Edition, A09 Addenda**

$$t_{w(\text{lower})} = 1 \text{ in}$$

$$\text{Leg}_{41} = 0.375 \text{ in}$$



Note: round inside edges per UG-76(c)

Located on:	Cylinder #1
Liquid static head included:	0 psi
Nozzle material specification:	SA-312 TP304 Wld & smls pipe (II-D p. 90, In. 15)
Nozzle longitudinal joint efficiency:	1
Nozzle description:	24" (Thk = 1.000")
Nozzle orientation:	0°
Local vessel minimum thickness:	0.875 in
Nozzle center line offset to datum line:	50 in
End of nozzle to shell center:	40 in
Nozzle inside diameter, new:	22 in
Nozzle nominal wall thickness:	1 in
Nozzle corrosion allowance:	0 in
Projection available outside vessel, Lpr:	28 in

Note: Nozzle is outside of scope of Appendix 1-7 as $R_n / R > 0.7$. Appendix 1-10 or Division 2 Part 4.5 was used for the U-2(g) large opening analysis.

This nozzle passes through a Category A joint.

Reinforcement Calculations for Internal Pressure

Available reinforcement per Appendix 1-10 governs the MAWP of this nozzle.

Appendix 1-10 Maximum Local Primary Membrane Stress For P = 710.48 psi @ 650 °F The opening is adequately reinforced							UG-45 Nozzle Wall Thickness Summary (in) The nozzle passes UG-45	
P _L (psi)	Sallow (psi)	A ₁ (in ²)	A ₂ (in ²)	A ₃ (in ²)	A ₅ (in ²)	A welds (in ²)	t _{req} (in)	t _{min} (in)
20.655	20.655	7.8721	3.462	--	--	0.0703	0.4955	0.875

Division 2 Part 4.5 Strength of Nozzle Attachment Welds Summary Average Shear Stress in Weld								
k _y	L _τ (in)	L _{41T} (in)	L _{42T} (in)	L _{43T} (in)	f _{welds} (lbf)	τ (psi)	S (psi)	Over stressed
1.0909	18.8496	0.2652	0	0	84.125.81	6.814	16,200	No

UW-16 Weld Sizing Summary			
Weld description	Required weld throat size (in)	Actual weld throat size (in)	Status
Nozzle to shell fillet (Leg ₄₁)	0.25	0.2625	weld size is adequate

Calculations for internal pressure 710.48 psi @ 650 °F

Nozzle rated MDMT per UHA-51(d)(1)(a) = -320 °F.

Appendix 1-10

Effective radius of the vessel

$$\begin{aligned}
 R_{\text{eff}} &= 0.5 \cdot D_i \\
 &= 0.5 \cdot 22 \\
 &= 11 \text{ in}
 \end{aligned}$$

Limit of reinforcement along the vessel wall

$$\begin{aligned}
 L_R &= 8 \cdot t \\
 &= 8 \cdot 0.875 \\
 &= 7 \text{ in}
 \end{aligned}$$

Limit of reinforcement along the nozzle wall projecting outside the vessel surface

$$\begin{aligned}
 L_{H1} &= t + 0.78 \cdot (R_n \cdot t_n)^{0.5} \\
 &= 0.875 + 0.78 \cdot (11 \cdot 1)^{0.5} \\
 &= 3.462 \text{ in}
 \end{aligned}$$

$$\begin{aligned}
 L_{H2} &= L_{pr1} + t \\
 &= 28 + 0.875 \\
 &= 28.875 \text{ in}
 \end{aligned}$$

$$\begin{aligned}
 L_{H3} &= 8 \cdot (t + t_e) \\
 &= 8 \cdot (0.875 + 0) \\
 &= 7 \text{ in}
 \end{aligned}$$

$$\begin{aligned}
 L_H &= \min[L_{H1}, L_{H2}, L_{H3}] \\
 &= \min[3.462, 28.875, 7] \\
 &= 3.462 \text{ in}
 \end{aligned}$$

Effective thickness

$$\begin{aligned}
 t_{\text{eff}} &= t \\
 &= 0.875 \text{ in}
 \end{aligned}$$

Total available area near the nozzle opening

$$\begin{aligned}
 \lambda &= \min[(2 \cdot R_n + t_n) / ((D_i + t_{\text{eff}}) \cdot t_{\text{eff}})^{0.5}, 10] \\
 &= \min[(2 \cdot 11 + 1) / ((22 + 0.875) \cdot 0.875)^{0.5}, 10] \\
 &= 5.1409
 \end{aligned}$$

$$\begin{aligned}
 A_1 &= t \cdot L_R \cdot \max[(\lambda / 4), 1] \\
 &= 0.875 \cdot 7 \cdot \max[(5.1409 / 4), 1] \\
 &= 0.875 \cdot 7 \cdot 1.2852 \\
 &= \underline{7.8721} \text{ in}^2
 \end{aligned}$$

$$\begin{aligned}
 A_2 &= t_n \cdot L_H \\
 &= 1 \cdot 3.462 \\
 &= \underline{3.462} \text{ in}^2
 \end{aligned}$$

$$\begin{aligned}
 A_{41} &= 0.5 \cdot L_{41}^2 \\
 &= 0.5 \cdot 0.375^2 \\
 &= \underline{0.0703} \text{ in}^2
 \end{aligned}$$

$$\begin{aligned}
 A_T &= A_1 + A_2 + A_{41} \\
 &= 7.8721 + 3.462 + 0.0703 \\
 &= 11.4044 \text{ in}^2
 \end{aligned}$$

Forces at nozzle to vessel intersection

$$f_N = P \cdot R_n \cdot (L_H - t)$$

$$= 710.48 * 11 * (3.462 - 0.875)$$

$$= 20,218 \text{ lb}_f$$

$$f_S = P * R_{\text{eff}} * (L_R + t_n)$$

$$= 710.48 * 11 * (7 + 1)$$

$$= 62,522.64 \text{ lb}_f$$

$$f_Y = P * R_{\text{eff}} * R_{\text{nc}}$$

$$= 710.48 * 11 * 11$$

$$= 85,968.63 \text{ lb}_f$$

Average local primary membrane stress

$$\sigma_{\text{avg}} = (f_N + f_S + f_Y) / A_T$$

$$= (20,218 + 62,522.64 + 85,968.63) / 11.4044$$

$$= 14,793 \text{ psi}$$

General primary membrane stress

$$\sigma_{\text{circ}} = P * R_{\text{eff}} / t_{\text{eff}}$$

$$= 710.48 * 11 / 0.875$$

$$= 8,932 \text{ psi}$$

Maximum local primary membrane stress at the nozzle intersection

$$P_L = \max[\{2 * \sigma_{\text{avg}} - \sigma_{\text{circ}}\}, \sigma_{\text{circ}}]$$

$$= \max[\{2 * 14,793 - 8,932\}, 8,932]$$

$$= 20.655 \text{ psi}$$

Allowable stress

$$S_{\text{allow}} = 1.5 * S * E$$

$$= 1.5 * 16,200 * 0.85$$

$$= 20,655 \text{ psi}$$

$$P_L = 20,655 \text{ psi} \leq S_{\text{allow}} = 20,655 \text{ psi} \quad \text{satisfactory}$$

Maximum allowable working pressure

$$A_p = R_n * (L_H - t) + R_{\text{eff}} * (L_R + t_n + R_{\text{nc}})$$

$$= (11 * (3.462 - 0.875) + 11 * (7 + 1 + 11))$$

$$= 237.4566 \text{ in}^2$$

$$P_{\text{max1}} = S_{\text{allow}} / (2 * A_p / A_T - R_{\text{eff}} / t_{\text{eff}})$$

$$= 20,655 / (2 * 237.4566 / 11.4044 - 11 / 0.875)$$

$$= 710.4845 \text{ psi}$$

$$P_{\text{max2}} = S * (t / R_{\text{eff}})$$

$$= 16,200 * (0.875 / 11)$$

$$= 1,288.636 \text{ psi}$$

$$\begin{aligned}
 P_{\max} &= \min[P_{\max1}, P_{\max2}] \\
 &= \min[710.48, 1,288.64] \\
 &= 710.4845 \text{ psi}
 \end{aligned}$$

Division 2 Part 4.5 Strength of Nozzle Attachment Welds (U-2(g) analysis)

Discontinuity force factor

$$\begin{aligned}
 k_y &= (R_{nc} + t_n) / R_{nc} \\
 &= (11 + 1) / 11 \\
 &= \underline{1.0909}
 \end{aligned}$$

Weld length resisting discontinuity force

$$\begin{aligned}
 L_\tau &= \pi / 2 * (R_n + t_n) \\
 &= \pi / 2 * (11 + 1) \\
 &= \underline{18.8496} \text{ in}
 \end{aligned}$$

Weld throat dimensions

$$\begin{aligned}
 L_{41T} &= 0.7071 * L_{41} \\
 &= 0.7071 * 0.375 \\
 &= \underline{0.2652} \text{ in}
 \end{aligned}$$

Average shear stress in weld

$$\begin{aligned}
 f_{\text{welds}} &= \min[f_y * k_y, 1.5 * S_n * (A_2 + A_3)] \\
 &= \min[85,968.63 * 1.0909, 1.5 * 16,200 * (3.462 + 0)] \\
 &= \underline{84,125.81} \text{ lb}_f
 \end{aligned}$$

$$\begin{aligned}
 \tau &= f_{\text{welds}} / [L_\tau * (0.49 * L_{41T} + 0.6 * t_{w1} + 0.49 * L_{43T})] \\
 &= 84,125.81 / [18.8496 * (0.49 * 0.2652 + 0.6 * 0.875 + 0.49 * 0)] \\
 &= \underline{6.814} \text{ psi}
 \end{aligned}$$

$$\tau = 6,814 \text{ psi} \leq S = 16,200 \text{ psi} \quad \text{satisfactory}$$

UW-16(c) Weld Check

Fillet weld: t_{\min} = lesser of 0.75 or t_n or $t = 0.75$ in

$t_{c(\min)}$ = lesser of 0.25 or $0.7 * t_{\min} = \underline{0.25}$ in

$t_{c(\text{actual})} = 0.7 * \text{Leg} = 0.7 * 0.375 = 0.2625$ in

The fillet weld size is satisfactory.

Weld strength calculations are not required for this detail which conforms to Fig. UW-16.1, sketch (c-e).

UG-45 Nozzle Neck Thickness Check

**Sample Project.
For information only.**

Wall thickness per UG-45(a): $t_{r1} = 0.4955$ in ($E = 1$)
Wall thickness per UG-45(b)(1): $t_{r2} = 0.5172$ in
Wall thickness per UG-16(b): $t_{r3} = 0.0625$ in
Standard wall pipe per UG-45(b)(4): $t_{r4} = 0.3281$ in
The greater of t_{r2} or t_{r3} : $t_{r5} = 0.5172$ in
The lesser of t_{r4} or t_{r5} : $t_{r6} = 0.3281$ in

Required per UG-45 is the larger of t_{r1} or $t_{r6} = 0.4955$ in

Available nozzle wall thickness new, $t_n = 0.875 \times 1 = 0.875$ in

The nozzle neck thickness is adequate.

Reinforcement Calculations for MAP

Available reinforcement per Appendix 1-10 governs the MAP of this nozzle.

Appendix 1-10 Maximum Local Primary Membrane Stress For P = 877.14 psi @ 70 °F The opening is adequately reinforced							UG-45 Nozzle Wall Thickness Summary (in) The nozzle passes UG-45	
P _L (psi)	Sallow (psi)	A ₁ (in ²)	A ₂ (in ²)	A ₃ (in ²)	A ₅ (in ²)	A welds (in ²)	t _{req} (in)	t _{min} (in)
25.500	25.500	7.8721	3.462	--	--	0.0703	0.4955	0.875

Division 2 Part 4.5 Strength of Nozzle Attachment Welds Summary Average Shear Stress in Weld								
k _y	L _τ (in)	L _{41T} (in)	L _{42T} (in)	L _{43T} (in)	f _{welds} (lbf)	τ (psi)	S (psi)	Over stressed
1.0909	18.8496	0.2652	0	0	103.859	8.413	20,000	No

UW-16 Weld Sizing Summary			
Weld description	Required weld throat size (in)	Actual weld throat size (in)	Status
Nozzle to shell fillet (Leg ₄₁)	0.25	0.2625	weld size is adequate

Calculations for internal pressure 877.14 psi @ 70 °F

Nozzle rated MDMT per UHA-51(d)(1)(a) = -320 °F.

Appendix 1-10

Effective radius of the vessel

$$\begin{aligned}
 R_{\text{eff}} &= 0.5 \cdot D_i \\
 &= 0.5 \cdot 22 \\
 &= 11 \text{ in}
 \end{aligned}$$

Limit of reinforcement along the vessel wall

$$\begin{aligned}
 L_R &= 8 \cdot t \\
 &= 8 \cdot 0.875 \\
 &= 7 \text{ in}
 \end{aligned}$$

Limit of reinforcement along the nozzle wall projecting outside the vessel surface

$$\begin{aligned}
 L_{H1} &= t + 0.78 \cdot (R_n \cdot t_n)^{0.5} \\
 &= 0.875 + 0.78 \cdot (11 \cdot 1)^{0.5} \\
 &= 3.462 \text{ in}
 \end{aligned}$$

$$\begin{aligned}
 L_{H2} &= L_{pr1} + t \\
 &= 28 + 0.875 \\
 &= 28.875 \text{ in}
 \end{aligned}$$

$$\begin{aligned}
 L_{H3} &= 8 \cdot (t + t_e) \\
 &= 8 \cdot (0.875 + 0) \\
 &= 7 \text{ in}
 \end{aligned}$$

$$\begin{aligned}
 L_H &= \min[L_{H1}, L_{H2}, L_{H3}] \\
 &= \min[3.462, 28.875, 7] \\
 &= 3.462 \text{ in}
 \end{aligned}$$

Effective thickness

$$\begin{aligned}
 t_{\text{eff}} &= t \\
 &= 0.875 \text{ in}
 \end{aligned}$$

Total available area near the nozzle opening

$$\begin{aligned}
 \lambda &= \min[(2 \cdot R_n + t_n) / ((D_i + t_{\text{eff}}) \cdot t_{\text{eff}})^{0.5}, 10] \\
 &= \min[(2 \cdot 11 + 1) / ((22 + 0.875) \cdot 0.875)^{0.5}, 10] \\
 &= 5.1409
 \end{aligned}$$

$$\begin{aligned}
 A_1 &= t \cdot L_R \cdot \max[(\lambda / 4), 1] \\
 &= 0.875 \cdot 7 \cdot \max[(5.1409 / 4), 1] \\
 &= 0.875 \cdot 7 \cdot 1.2852 \\
 &= \underline{7.8721} \text{ in}^2
 \end{aligned}$$

$$\begin{aligned}
 A_2 &= t_n \cdot L_H \\
 &= 1 \cdot 3.462 \\
 &= \underline{3.462} \text{ in}^2
 \end{aligned}$$

$$\begin{aligned}
 A_{41} &= 0.5 \cdot L_{41}^2 \\
 &= 0.5 \cdot 0.375^2 \\
 &= \underline{0.0703} \text{ in}^2
 \end{aligned}$$

$$\begin{aligned}
 A_T &= A_1 + A_2 + A_{41} \\
 &= 7.8721 + 3.462 + 0.0703 \\
 &= 11.4044 \text{ in}^2
 \end{aligned}$$

Forces at nozzle to vessel intersection

$$f_N = P \cdot R_n \cdot (L_H - t)$$

$$= 877.14 * 11 * (3.462 - 0.875)$$

$$= 24,960.49 \text{ lb}_f$$

$$f_S = P * R_{\text{eff}} * (L_R + t_n)$$

$$= 877.14 * 11 * (7 + 1)$$

$$= 77,188.44 \text{ lb}_f$$

$$f_Y = P * R_{\text{eff}} * R_{\text{nc}}$$

$$= 877.14 * 11 * 11$$

$$= 106,134.1 \text{ lb}_f$$

Average local primary membrane stress

$$\sigma_{\text{avg}} = (f_N + f_S + f_Y) / A_T$$

$$= (24,960.49 + 77,188.44 + 106,134.1) / 11.4044$$

$$= 18,263 \text{ psi}$$

General primary membrane stress

$$\sigma_{\text{circ}} = P * R_{\text{eff}} / t_{\text{eff}}$$

$$= 877.14 * 11 / 0.875$$

$$= 11,027 \text{ psi}$$

Maximum local primary membrane stress at the nozzle intersection

$$P_L = \max[\{2 * \sigma_{\text{avg}} - \sigma_{\text{circ}}\}, \sigma_{\text{circ}}]$$

$$= \max[\{2 * 18,263 - 11,027\}, 11,027]$$

$$= \underline{25,500} \text{ psi}$$

Allowable stress

$$S_{\text{allow}} = 1.5 * S * E$$

$$= 1.5 * 20,000 * 0.85$$

$$= 25,500 \text{ psi}$$

$$P_L = 25,500 \text{ psi} \leq S_{\text{allow}} = 25,500 \text{ psi} \quad \text{satisfactory}$$

Maximum allowable pressure

$$A_p = R_n * (L_H - t) + R_{\text{eff}} * (L_R + t_n + R_{\text{nc}})$$

$$= (11 * (3.462 - 0.875) + 11 * (7 + 1 + 11))$$

$$= 237.4566 \text{ in}^2$$

$$P_{\text{max1}} = S_{\text{allow}} / (2 * A_p / A_T - R_{\text{eff}} / t_{\text{eff}})$$

$$= 25,500 / (2 * 237.4566 / 11.4044 - 11 / 0.875)$$

$$= 877.1413 \text{ psi}$$

$$P_{\text{max2}} = S * (t / R_{\text{eff}})$$

$$= 20,000 * (0.875 / 11)$$

$$= 1,590.909 \text{ psi}$$

$$\begin{aligned}
 P_{\max} &= \min[P_{\max1}, P_{\max2}] \\
 &= \min[877.14, 1,590.91] \\
 &= 877.1413 \text{ psi}
 \end{aligned}$$

Division 2 Part 4.5 Strength of Nozzle Attachment Welds (U-2(g) analysis)

Discontinuity force factor

$$\begin{aligned}
 k_y &= (R_{nc} + t_n) / R_{nc} \\
 &= (11 + 1) / 11 \\
 &= \underline{1.0909}
 \end{aligned}$$

Weld length resisting discontinuity force

$$\begin{aligned}
 L_\tau &= \pi / 2 * (R_n + t_n) \\
 &= \pi / 2 * (11 + 1) \\
 &= \underline{18.8496} \text{ in}
 \end{aligned}$$

Weld throat dimensions

$$\begin{aligned}
 L_{41T} &= 0.7071 * L_{41} \\
 &= 0.7071 * 0.375 \\
 &= \underline{0.2652} \text{ in}
 \end{aligned}$$

Average shear stress in weld

$$\begin{aligned}
 f_{\text{welds}} &= \min[f_y * k_y, 1.5 * S_n * (A_2 + A_3)] \\
 &= \min[106,134.1 * 1.0909, 1.5 * 20,000 * (3.462 + 0)] \\
 &= \underline{103.859} \text{ lb}_f
 \end{aligned}$$

$$\begin{aligned}
 \tau &= f_{\text{welds}} / [L_\tau * (0.49 * L_{41T} + 0.6 * t_{w1} + 0.49 * L_{43T})] \\
 &= 103,859 / [18.8496 * (0.49 * 0.2652 + 0.6 * 0.875 + 0.49 * 0)] \\
 &= \underline{8.413} \text{ psi}
 \end{aligned}$$

$$\tau = 8,413 \text{ psi} \leq S = 20,000 \text{ psi} \quad \text{satisfactory}$$

UW-16(c) Weld Check

Fillet weld: t_{\min} = lesser of 0.75 or t_n or $t = 0.75$ in

$t_{c(\min)}$ = lesser of 0.25 or $0.7 * t_{\min} = \underline{0.25}$ in

$t_{c(\text{actual})} = 0.7 * \text{Leg} = 0.7 * 0.375 = 0.2625$ in

The fillet weld size is satisfactory.

Weld strength calculations are not required for this detail which conforms to Fig. UW-16.1, sketch (c-e).

UG-45 Nozzle Neck Thickness Check

Wall thickness per UG-45(a): $t_{r1} = 0.4955$ in ($E = 1$)
Wall thickness per UG-45(b)(1): $t_{r2} = 0.5172$ in
Wall thickness per UG-16(b): $t_{r3} = 0.0625$ in
Standard wall pipe per UG-45(b)(4): $t_{r4} = 0.3281$ in
The greater of t_{r2} or t_{r3} : $t_{r5} = 0.5172$ in
The lesser of t_{r4} or t_{r5} : $t_{r6} = 0.3281$ in

Required per UG-45 is the larger of t_{r1} or $t_{r6} = 0.4955$ in

Available nozzle wall thickness new, $t_n = 0.875 \times 1 = 0.875$ in

The nozzle neck thickness is adequate.

Reinforcement Calculations for External Pressure

Appendix 1-10 Maximum Local Primary Membrane Stress For $P_e = 282.83$ psi @ 650 °F The opening is adequately reinforced							UG-45 Nozzle Wall Thickness Summary (in) The nozzle passes UG-45	
P_L (psi)	Sallow (psi)	A_1 (in ²)	A_2 (in ²)	A_3 (in ²)	A_5 (in ²)	A welds (in ²)	t_{req} (in)	t_{min} (in)
10.353	10.353	6.125	3.462	--	--	0.0703	0.6652	0.875

Division 2 Part 4.5 Strength of Nozzle Attachment Welds Summary Average Shear Stress in Weld								
k_y	L_τ (in)	L_{41T} (in)	L_{42T} (in)	L_{43T} (in)	f_{welds} (lbf)	τ (psi)	S (psi)	Over stressed
1.0909	18.8496	0.2652	0	0	37.333.93	3.024	16,200	No

UW-16 Weld Sizing Summary			
Weld description	Required weld throat size (in)	Actual weld throat size (in)	Status
Nozzle to shell fillet (Leg ₄₁)	0.25	0.2625	weld size is adequate

Calculations for external pressure 282.83 psi @ 650 °F

Appendix 1-10

Effective radius of the vessel

$$\begin{aligned}
 R_{eff} &= 0.5 \cdot D_i \\
 &= 0.5 \cdot 22 \\
 &= 11 \text{ in}
 \end{aligned}$$

Limit of reinforcement along the vessel wall

$$\begin{aligned}
 L_R &= 8 \cdot t \\
 &= 8 \cdot 0.875 \\
 &= 7 \text{ in}
 \end{aligned}$$

Limit of reinforcement along the nozzle wall projecting outside the vessel surface

$$\begin{aligned}
 L_{H1} &= t + 0.78 \cdot (R_n \cdot t_n)^{0.5} \\
 &= 0.875 + 0.78 \cdot (11 \cdot 1)^{0.5} \\
 &= 3.462 \text{ in}
 \end{aligned}$$

$$\begin{aligned}
 L_{H2} &= L_{pr1} + t \\
 &= 28 + 0.875 \\
 &= 28.875 \text{ in}
 \end{aligned}$$

$$\begin{aligned}
 L_{H3} &= 8 \cdot (t + t_e) \\
 &= 8 \cdot (0.875 + 0) \\
 &= 7 \text{ in}
 \end{aligned}$$

$$\begin{aligned}
 L_H &= \min[L_{H1}, L_{H2}, L_{H3}] \\
 &= \min[3.462, 28.875, 7] \\
 &= 3.462 \text{ in}
 \end{aligned}$$

Effective thickness

$$\begin{aligned}
 t_{\text{eff}} &= t \\
 &= 0.875 \text{ in}
 \end{aligned}$$

Total available area near the nozzle opening

$$\lambda = 0 \text{ (for external pressure design)}$$

$$\begin{aligned}
 A_1 &= t \cdot L_R \cdot \max[(\lambda / 4), 1] \\
 &= 0.875 \cdot 7 \cdot \max[(0 / 4), 1] \\
 &= 0.875 \cdot 7 \cdot 1 \\
 &= \underline{6.125} \text{ in}^2
 \end{aligned}$$

$$\begin{aligned}
 A_2 &= t_n \cdot L_H \\
 &= 1 \cdot 3.462 \\
 &= \underline{3.462} \text{ in}^2
 \end{aligned}$$

$$\begin{aligned}
 A_{41} &= 0.5 \cdot L_{41}^2 \\
 &= 0.5 \cdot 0.375^2 \\
 &= \underline{0.0703} \text{ in}^2
 \end{aligned}$$

$$\begin{aligned}
 A_T &= A_1 + A_2 + A_{41} \\
 &= 6.125 + 3.462 + 0.0703 \\
 &= 9.6573 \text{ in}^2
 \end{aligned}$$

Forces at nozzle to vessel intersection

$$\begin{aligned}
 f_N &= P \cdot R_n \cdot (L_H - t) \\
 &= 282.83 \cdot 11 \cdot (3.462 - 0.875) \\
 &= 8,048.47 \text{ lb}_f
 \end{aligned}$$

$$f_S = P \cdot R_{\text{eff}} \cdot (L_R + t_n)$$

$$= 282.83 * 11 * (7 + 1)$$

$$= 24,889.29 \text{ lb}_f$$

$$f_Y = P * R_{\text{eff}} * R_{\text{nc}}$$

$$= 282.83 * 11 * 11$$

$$= 34,222.77 \text{ lb}_f$$

Average local primary membrane stress

$$\sigma_{\text{avg}} = (f_N + f_S + f_Y) / A_T$$

$$= (8,048.47 + 24,889.29 + 34,222.77) / 9.6573$$

$$= 6,954 \text{ psi}$$

General primary membrane stress

$$\sigma_{\text{circ}} = P * R_{\text{eff}} / t_{\text{eff}}$$

$$= 282.83 * 11 / 0.875$$

$$= 3,556 \text{ psi}$$

Maximum local primary membrane stress at the nozzle intersection

$$P_L = \max[\{2 * \sigma_{\text{avg}} - \sigma_{\text{circ}}\}, \sigma_{\text{circ}}]$$

$$= \max[\{2 * 6,954 - 3,556\}, 3,556]$$

$$= 10.353 \text{ psi}$$

Allowable stress

$$S_{\text{allow}} = 1.5 * \min[S_C, S]$$

$$= 1.5 * \min[6,902, 16,200]$$

$$= 10,353 \text{ psi}$$

$$P_L = 10,353 \text{ psi} \leq S_{\text{allow}} = 10,353 \text{ psi} \quad \text{satisfactory}$$

Maximum allowable external pressure

$$A_p = R_n * (L_H - t) + R_{\text{eff}} * (L_R + t_n + R_{\text{nc}})$$

$$= (11 * (3.462 - 0.875) + 11 * (7 + 1 + 11))$$

$$= 237.4566 \text{ in}^2$$

$$P_{\text{max1}} = S_{\text{allow}} / (2 * A_p / A_T - R_{\text{eff}} / t_{\text{eff}})$$

$$= 10,353 / (2 * 237.4566 / 9.6573 - 11 / 0.875)$$

$$= 282.8328 \text{ psi}$$

$$P_{\text{max2}} = S * (t / R_{\text{eff}})$$

$$= 6,902 * (0.875 / 11)$$

$$= 549.032 \text{ psi}$$

$$P_{\text{max}} = \min[P_{\text{max1}}, P_{\text{max2}}]$$

$$= \min[282.83, 549.03]$$

$$= 282.8328 \text{ psi}$$

Division 2 Part 4.5 Strength of Nozzle Attachment Welds (U-2(g) analysis)**Discontinuity force factor**

$$\begin{aligned}
 k_y &= (R_{nc} + t_n) / R_{nc} \\
 &= (11 + 1) / 11 \\
 &= \underline{1.0909}
 \end{aligned}$$

Weld length resisting discontinuity force

$$\begin{aligned}
 L_\tau &= \pi / 2 * (R_n + t_n) \\
 &= \pi / 2 * (11 + 1) \\
 &= \underline{18.8496} \text{ in}
 \end{aligned}$$

Weld throat dimensions

$$\begin{aligned}
 L_{41T} &= 0.7071 * L_{41} \\
 &= 0.7071 * 0.375 \\
 &= \underline{0.2652} \text{ in}
 \end{aligned}$$

Average shear stress in weld

$$\begin{aligned}
 f_{welds} &= \min[f_y * k_y, 1.5 * S_n * (A_2 + A_3)] \\
 &= \min[34,222.77 * 1.0909, 1.5 * 16,200 * (3.462 + 0)] \\
 &= \underline{37,333.93} \text{ lb}_f
 \end{aligned}$$

$$\begin{aligned}
 \tau &= f_{welds} / [L_\tau * (0.49 * L_{41T} + 0.6 * t_{w1} + 0.49 * L_{43T})] \\
 &= 37,333.93 / [18.8496 * (0.49 * 0.2652 + 0.6 * 0.875 + 0.49 * 0)] \\
 &= \underline{3.024} \text{ psi}
 \end{aligned}$$

$$\tau = 3,024 \text{ psi} \leq S = 16,200 \text{ psi} \quad \text{satisfactory}$$

UW-16(c) Weld Check

Fillet weld: t_{min} = lesser of 0.75 or t_n or $t = 0.75$ in

$t_{c(min)}$ = lesser of 0.25 or $0.7 * t_{min} = \underline{0.25}$ in

$t_{c(actual)}$ = $0.7 * \text{Leg} = 0.7 * 0.375 = 0.2625$ in

The fillet weld size is satisfactory.

Weld strength calculations are not required for this detail which conforms to Fig. UW-16.1, sketch (c-e).

UG-45 Nozzle Neck Thickness Check

Wall thickness per UG-45(a): $t_{r1} = 0.6652$ in

Wall thickness per UG-45(b)(2): $t_{r2} = 0.2081$ in

Wall thickness per UG-16(b): $t_{r3} = 0.0625$ in

Standard wall pipe per UG-45(b)(4): $t_{r4} = 0.3281$ in

The greater of t_{r2} or t_{r3} : $t_{r5} = 0.2081$ in

The lesser of t_{r4} or t_{r5} : $t_{r6} = 0.2081$ in

Required per UG-45 is the larger of t_{r1} or $t_{r6} = 0.6652$ in

Available nozzle wall thickness new, $t_n = 0.875 \times 1 = 0.875$ in

The nozzle neck thickness is adequate.

External Pressure, (Corroded & at 650 °F) UG-28(c)

$$L / D_o = 40 / 24 = 1.6667$$

$$D_o / t = 24 / 0.6652 = 36.0787$$

From table G: $A = 0.003732$

From table HA-1: $B = 7,653$ psi

$$\begin{aligned} P_a &= 4*B / (3*(D_o / t)) \\ &= 4*7653.1895 / (3*(24 / 0.6652)) \\ &= 282.83 \text{ psi} \end{aligned}$$

Design thickness for external pressure $P_a = 282.83$ psi

$$t_a = t + \text{Corrosion} = 0.6652 + 0 = 0.6652''$$